

$$P(\emptyset) = \{\emptyset\}$$

$$P(P(\emptyset)) = \{\emptyset, \{\emptyset\}\}$$

$$P(P(P(\emptyset))) = \{\emptyset, \{\emptyset\}, \{\{\emptyset\}\}, \{\emptyset, \{\emptyset\}\}\}$$

$$P(P(P(P(\emptyset)))) = \{\emptyset, \{\emptyset\}, \{\{\emptyset\}\}, \{\{\emptyset, \{\emptyset\}\}\},$$

$$\{\emptyset, \{\emptyset\}\}, \{\emptyset, \{\{\emptyset\}\}\}, \{\emptyset, \{\emptyset, \{\emptyset\}\}\},$$

$$\{\{\emptyset\}, \{\{\emptyset\}\}\}, \{\{\emptyset\}, \{\emptyset, \{\emptyset\}\}\}, \{\{\emptyset\}, \{\emptyset, \{\{\emptyset\}\}\}\},$$

$$\{\emptyset, \{\{\emptyset\}, \{\{\emptyset\}\}\}\}, \{\emptyset, \{\emptyset\}, \{\emptyset, \{\{\emptyset\}\}\}\},$$

$$\{\emptyset, \{\{\emptyset\}\}, \{\emptyset, \{\{\emptyset\}\}\}\}, \{\{\emptyset\}, \{\{\emptyset\}\}, \{\emptyset, \{\{\emptyset\}\}\}\},$$

$$\{\emptyset, \{\{\emptyset\}, \{\{\emptyset\}\}, \{\emptyset, \{\{\emptyset\}\}\}\}\}$$

$$V = \{0, 1\}$$

$$P(V) = \{\emptyset, \{0\}, \{1\}, \{0, 1\}\}$$

$$P(P(V)) = \{\emptyset, \{\emptyset\}, \{\{0\}\}, \{\{1\}\}, \{\{0, 1\}\},$$

$$\{\emptyset, \{0\}\}, \{\emptyset, \{1\}\}, \{\emptyset, \{0, 1\}\},$$

$$\{\{0\}, \{1\}\}, \{\{0\}, \{0, 1\}\}, \{\{1\}, \{0, 1\}\},$$

$$\{\emptyset, \{0\}, \{1\}\}, \{\emptyset, \{0\}, \{0, 1\}\},$$

$$\{\emptyset, \{1\}, \{0, 1\}\}, \{\{0\}, \{1\}, \{0, 1\}\},$$

$$\{\emptyset, \{0\}, \{1\}, \{0, 1\}\} ?$$

$$8) a. (V \cap W) \cap (V \cup W) =$$

$$((V \cap W) \cap V) \cup ((V \cap W) \cap W) = \text{(distributiviteit)}$$

$$(W \cap V) \cap V \cup (V \cap W) \cap W = \text{(commutativiteit)}$$

$$(W \cap (V \cap V)) \cup (V \cap (W \cap W)) = \text{(2x associativiteit)}$$

$$(W \cap V) \cup (V \cap W) = \text{(2x idempotentie)}$$

$$(V \cap W) \cup (V \cap W) = \text{(commutativiteit)}$$

$$V \cap W \quad \text{(idempotentie)}$$

$$b. ((A \cup B^c) \cap C) \cup ((B \cap A^c) \cap C) =$$

$$((A \cup B^c) \cap C) \cup ((B \cap A^c) \cap C) = \text{(def -)}$$

(2x comm)

$$C \cap ((A \cup B^c) \cup (B \cap A^c)) = \text{(distr)}$$

$$(C \cap (A \cup B^c)) \cup (C \cap (B \cap A^c)) =$$

$$C \cap (((A \cup B^c) \cup B) \cap ((A \cup B^c) \cup A^c)) = \text{(distr)}$$

$$C \cap (((A \cup B^c) \cup B) \cap ((B^c \cup A) \cup A^c)) = \text{(comm)}$$

$$C \cap ((A \cup (B^c \cup B)) \cap (B^c \cup (A \cup A^c))) = \text{(2x ass)}$$

$$C \cap ((A \cup U) \cap (B^c \cup U)) = \text{(2x compl)}$$

$$C \cap (U \cap U) = \text{(ident)}$$

$$C \cap U = \text{(idem)}$$

$$C \quad \text{(ident)}$$

9) a. Nee; tegenvoorbeeld:

$$A = \{a, b\}$$

$$B = \{a\}$$

$$C = \{b\}$$

$$A \cup B = \{a, b\} = A \cup C$$

maar $\{a\} \neq \{b\}$.

$$A = \{a, b\}$$

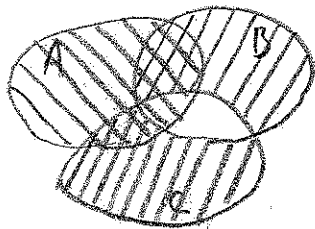
$$B = \{a, c\}$$

$$C = \{a, d\}$$

$$A \cap B = \{a\} = A \cap C$$

maar $\{a, b\} \neq \{a, d\}$

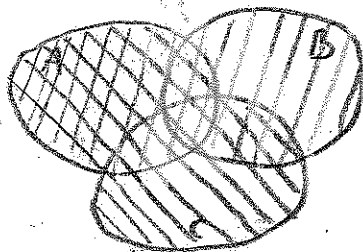
b.



$$B \oplus C = \text{diagonal lines}$$

$$A = \text{vertical lines}$$

$$A \cup (B \oplus C) = \text{vertical lines} + \text{diagonal lines} + \text{cross-hatch}$$



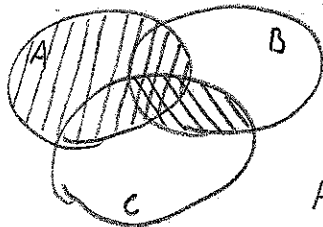
$$A \cup B = \text{diagonal lines}$$

$$A \cup C = \text{vertical lines}$$

$$(A \cup B) \oplus (A \cup C) = \text{diagonal lines} + \text{vertical lines}$$

das $A \cup (B \oplus C) \neq (A \cup B) \oplus (A \cup C)$: \cup distribueert niet over \oplus

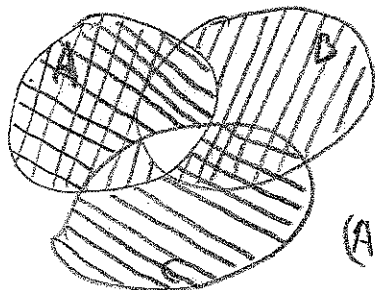
c.



$$A = \text{vertical lines}$$

$$B \cap C = \text{diagonal lines}$$

$$A \oplus (B \cap C) = \text{vertical lines} + \text{diagonal lines}$$



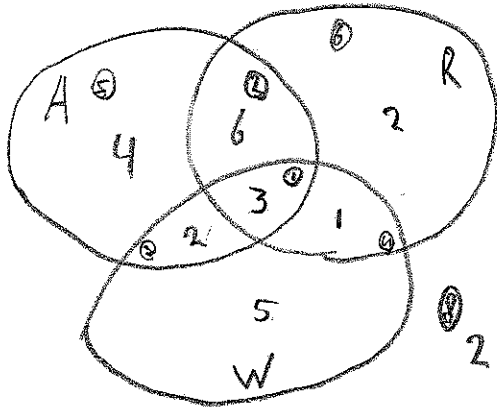
$$A \oplus B = \text{diagonal lines}$$

$$A \oplus C = \text{vertical lines}$$

$$(A \oplus B) \cap (A \oplus C) = \text{cross-hatch}$$

das $A \oplus (B \cap C) \neq (A \oplus B) \cap (A \oplus C)$: \oplus distribueert niet over \cap

10)



$$n(A) = 15$$

$$n(R) = 12$$

$$n(W) = 11$$

$$n(A \cap R) = 9$$

$$n(A \cap W) = 5$$

$$n(R \cap W) = 4$$

$$n(A \cap R \cap W) = 3$$

① $n(A \cap R \cap W)$ neteen invullen.

$$\textcircled{2} n(A \cap R) - n(A \cap R \cap W) = 9 - 3 = 6$$

$$\textcircled{3} n(A \cap W) - n(A \cap R \cap W) = 5 - 3 = 2$$

$$\textcircled{4} n(R \cap W) - n(A \cap R \cap W) = 4 - 3 = 1$$

$$\textcircled{5} n(A) - \textcircled{2} - \textcircled{3} - \textcircled{4} = 15 - 3 - 6 - 2 = 4$$

$$\textcircled{6} n(R) - \textcircled{2} - \textcircled{4} - \textcircled{5} = 12 - 3 - 6 - 1 = 2$$

$$\textcircled{7} n(W) - \textcircled{3} - \textcircled{4} - \textcircled{6} = 11 - 3 - 2 - 1 = 5$$

$$\textcircled{8} 25 - \textcircled{2} - \textcircled{3} - \textcircled{4} - \textcircled{5} - \textcircled{6} - \textcircled{7} = 25 - 3 - 6 - 2 - 1 - 4 - 2 - 5 = 2$$

a. 5

b. 4

c. 2

d. 1

e. 6

f. $4 + 2 + 5 = 11$ g. $25 - 2 = 23$

h. 2

ii) Thm. 1.5: $n(A \cup B) = n(A) + n(B) - n(A \cap B)$

$$n(A \cup B \cup C) =$$

$$n(A \cup (B \cup C)) =$$

$$n(A) + n(B \cup C) - n(A \cap (B \cup C)) = \text{(Thm. 1.5)}$$

$$n(A) + n(B) + n(C) - n(B \cap C) - n(A \cap (B \cup C)) = \text{(Thm. 1.5)}$$

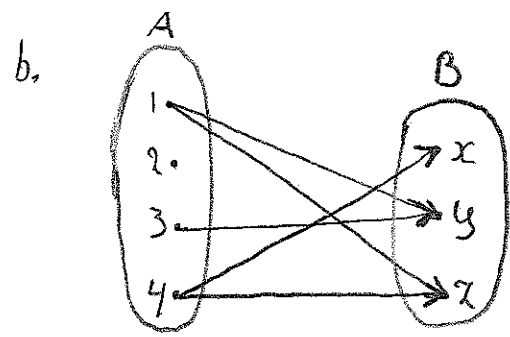
$$n(A) + n(B) + n(C) - n(B \cap C) - n((A \cap B) \cup (A \cap C)) = \text{(distrib)}$$

$$n(A) + n(B) + n(C) - n(B \cap C) - (n(A \cap B) + n(A \cap C) - n((A \cap B) \cap (A \cap C))) = \text{(Thm. 1.5)}$$

$$n(A) + n(B) + n(C) - n(B \cap C) - n(A \cap B) - n(A \cap C) + n(A \cap B \cap C) \quad \blacksquare$$

12) a.

	x	y	z
1	0	1	1
2	0	0	0
3	0	1	0
4	1	0	1



c. $R^{-1} = \{(y,1), (z,1), (y,3), (x,4), (z,4)\}$

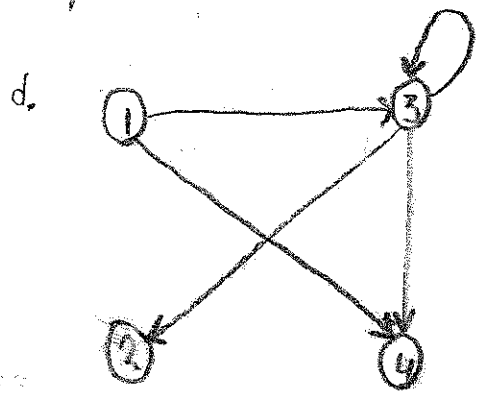
d. $D = \{1,3,4\}, R = \{x,y,z\}$

13) a.

	1	2	3	4
1	0	0	1	1
2	0	0	0	0
3	0	1	1	1
4	0	0	0	0

b. $D = \{1,3\}, R = \{2,3,4\}$

c. $R^{-1} = \{(3,1), (4,1), (2,3), (3,3), (4,3)\}$



e. $R \circ R = \{(1,2), (1,3), (1,4), (3,2), (3,3), (3,4)\}$

f. $R^{-1} \circ R = \{(2,2), (2,3), (2,4), (3,2), (3,3), (3,4), (4,2), (4,3), (4,4)\}$

$R \circ R^{-1} = \{(1,1), (1,3), (3,1), (3,3)\}$