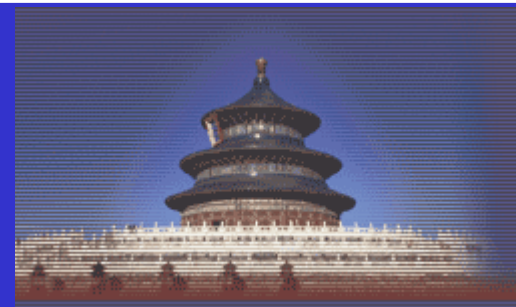




XML Transformation
by
Tree-Walking Transducers
with
Invisible Pebbles

Joost Engelfriet
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Bart Samwel
(Leiden University, NL)



PODS Beijing June 2007

tree model

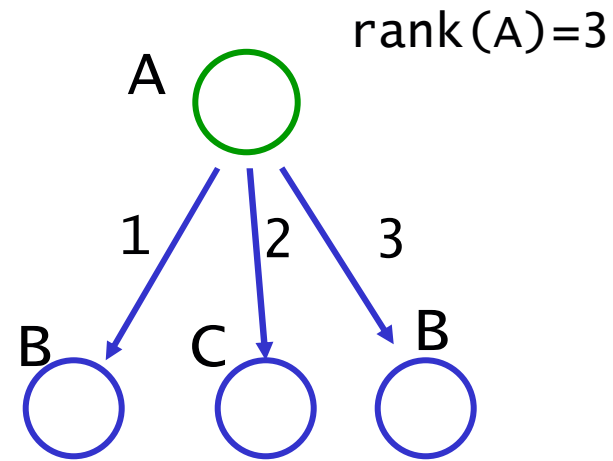
<A>

 ...

<C> ...

</C>

 ...



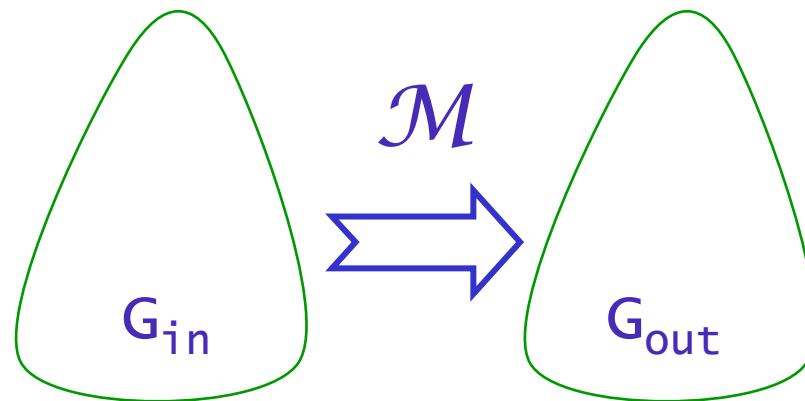
ranked trees

node labels with rank

unbounded number of children
(forests) are to be coded

typechecking

decide whether tree (document) generated by transformation \mathcal{M} satisfies description



Milo Suciú Vianu PODS2000

type checking for XML transformers is decidable

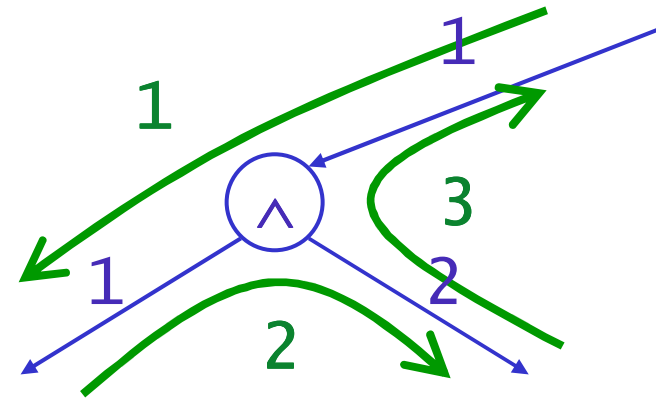
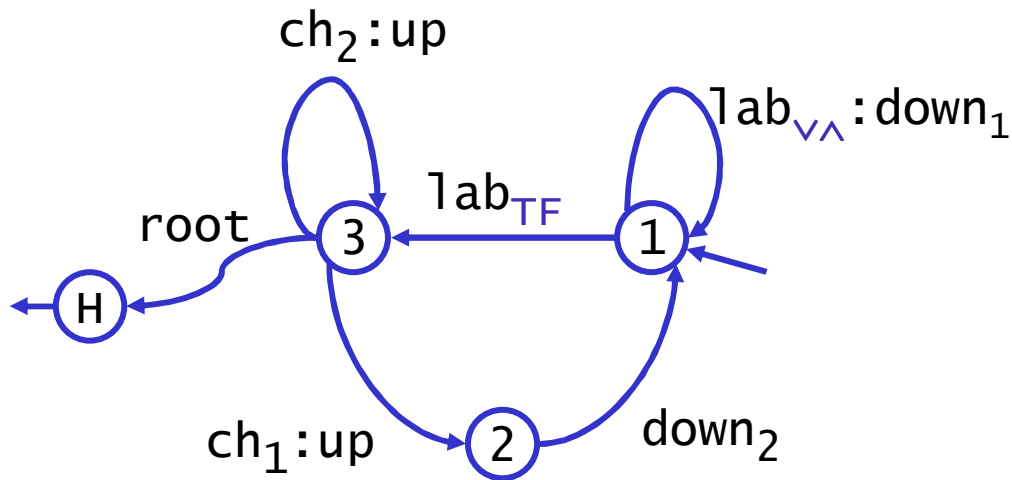
transformers with ‘visible’ pebbles:
finite number of coloured markers on tree

1. automata with pebbles
2. decomposition
3. typechecking
4. regular trees
5. document navigation
6. pattern matching
7. conclusion



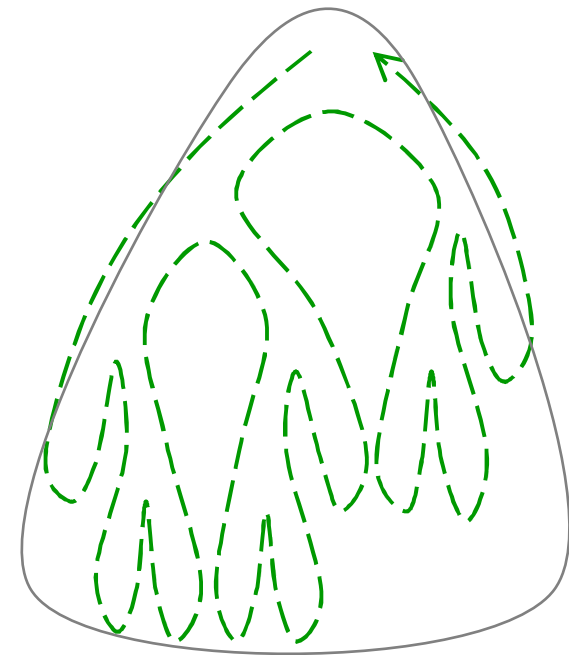
without pebbles

example: preorder tree traversal



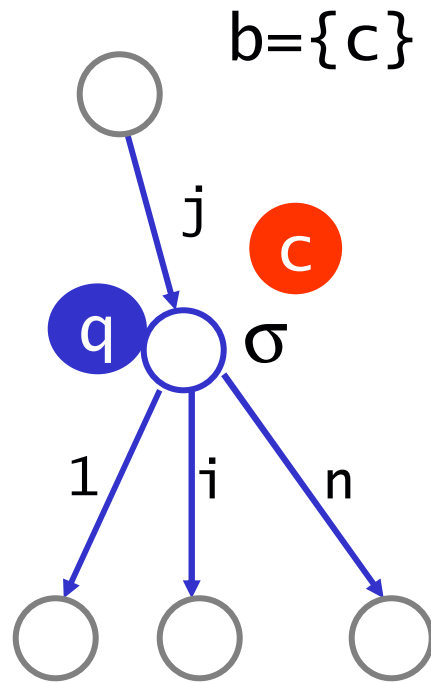
walk along edges, moves based on

- state
- node label
- child number
(= incoming edge)



tree-walking automata

with pebbles



local configuration

q state

σ node label

j child number

$j=0$ root

b pebble colours

$b \subseteq C$

instructions

$(q, \sigma, b, j) \rightarrow$

(halt)

(q', stay)

(q', up)

(q', down_j)

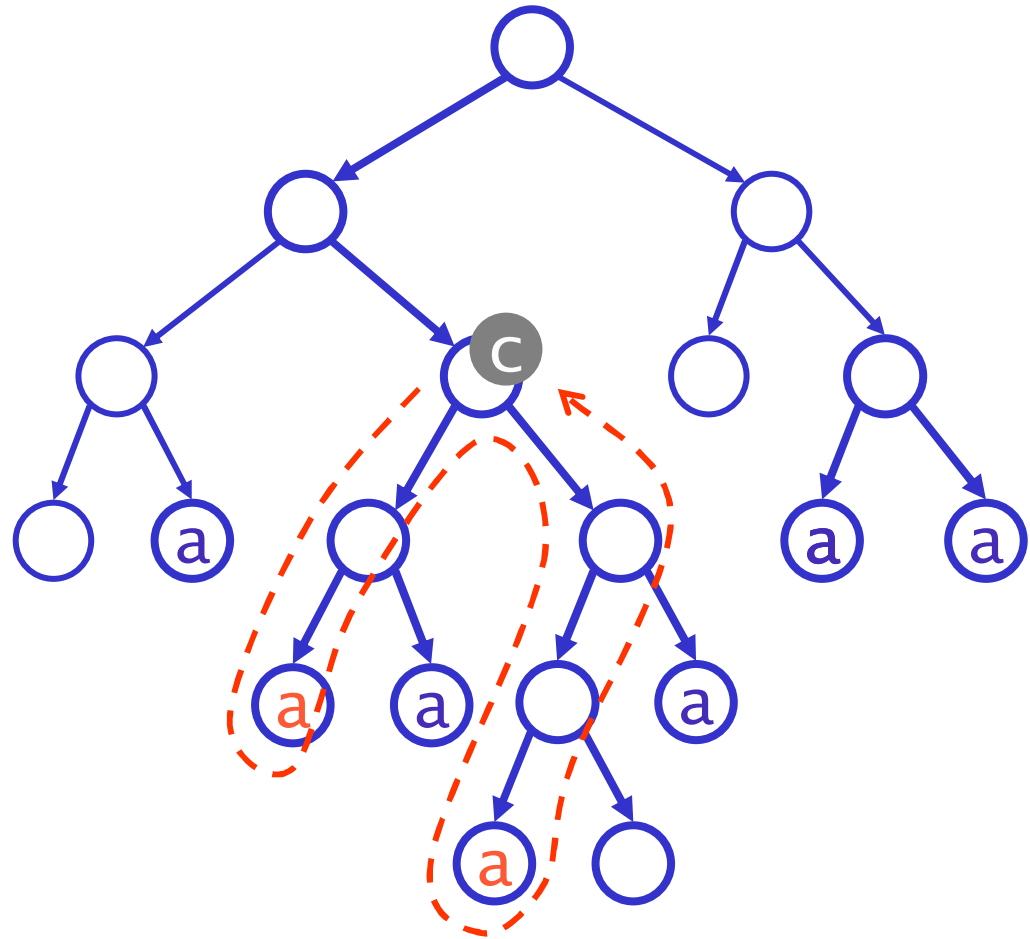
(q', drop_c)

(q', lift_c)

- finite set C of pebbles
- nested lifetimes
 - stack behaviour
 - only topmost can be lifted
- all observable

example: inspecting a subtree

using a pebble



tree-walking pebble automata

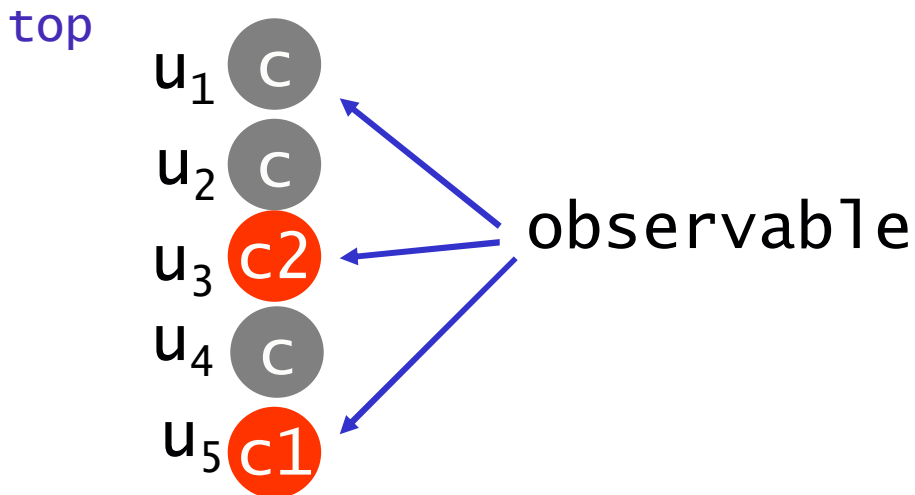
Ⓒ with *visible* pebbles
'colours' used once
always observable

☹ do not recognize all
regular tree languages
≡ MSO properties

Ⓒ we add *invisible* pebbles
colours used many times
only topmost is observable

☺ recognize regular
& decidable type checking
& better complexity

stack behaviour of pebbles!
(avoid 'counting')

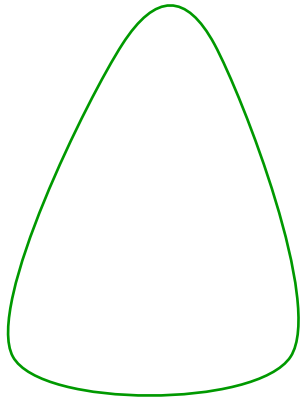


$(q, \sigma, b, j) \rightarrow (q', \text{stay})$

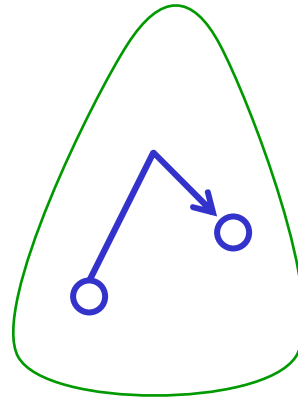
b contains

- all visible pebbles
- invisible when topmost

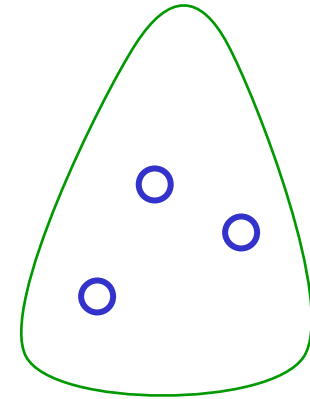
automaton defines ...



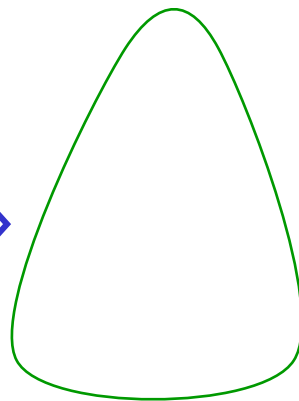
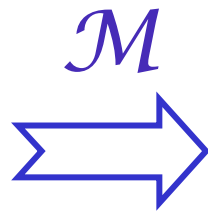
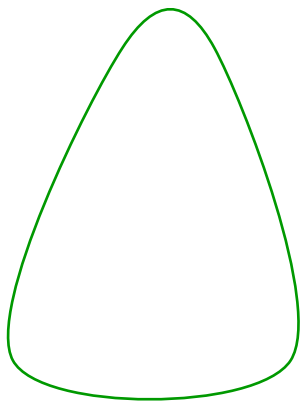
validation



navigation



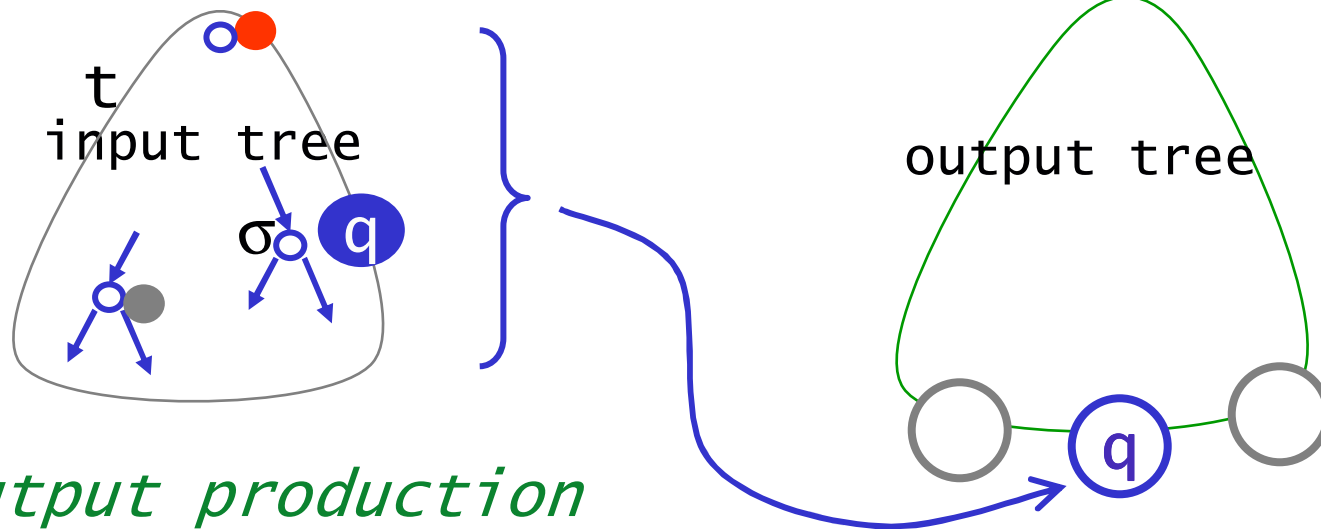
pattern
matching



transformation

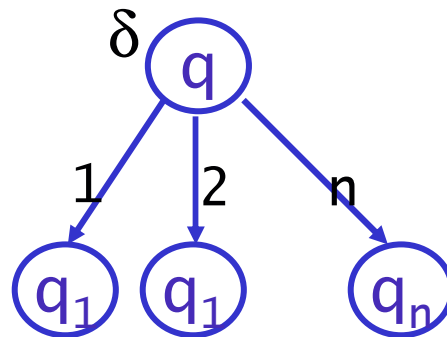
tree-walking pebble tree *transducers*

recursively generate output



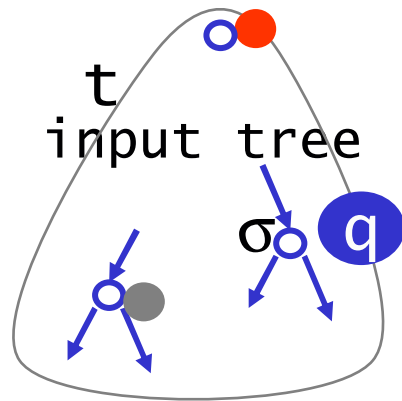
output production

$$(q, \sigma, b, j) \rightarrow \delta(q_1, q_2 \dots q_n)$$



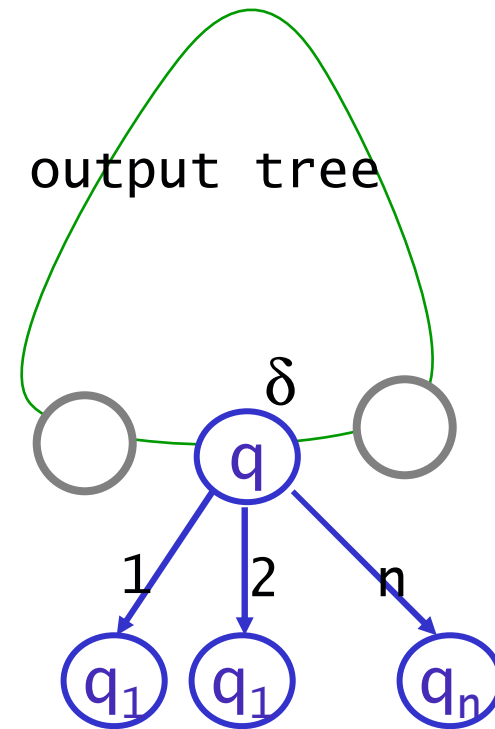
tree-walking pebble tree transducers

recursively generate output



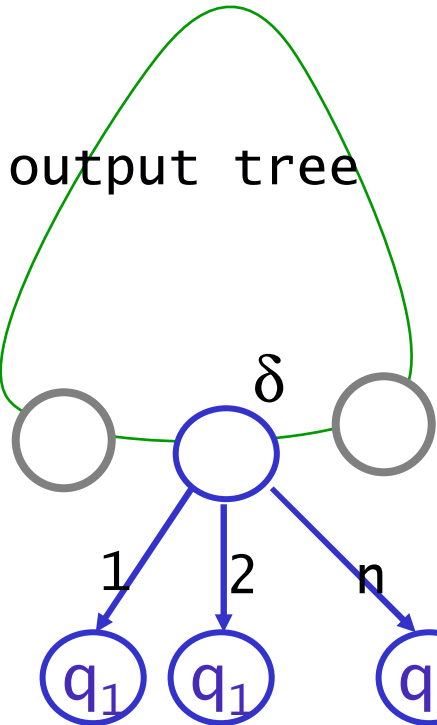
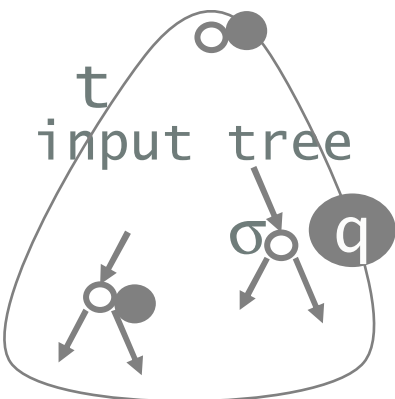
output production

$$(q, \sigma, b, j) \rightarrow \delta(q_1, q_2 \dots q_n)$$



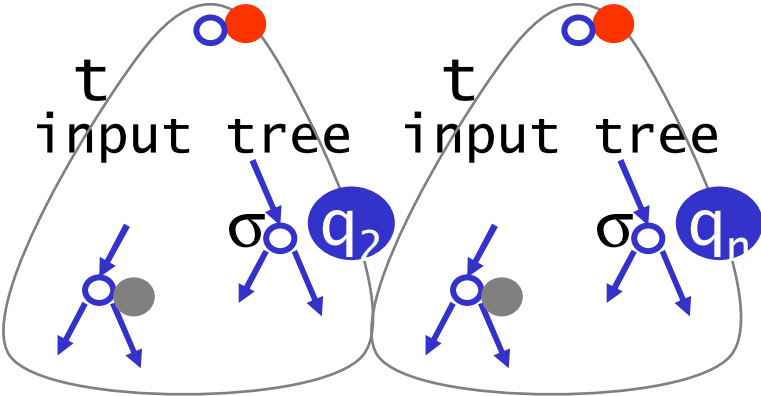
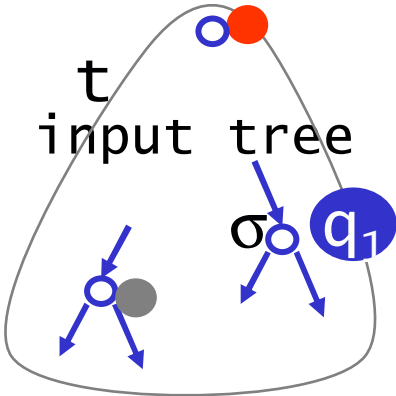
tree-walking pebble tree transducers

recursively generate output

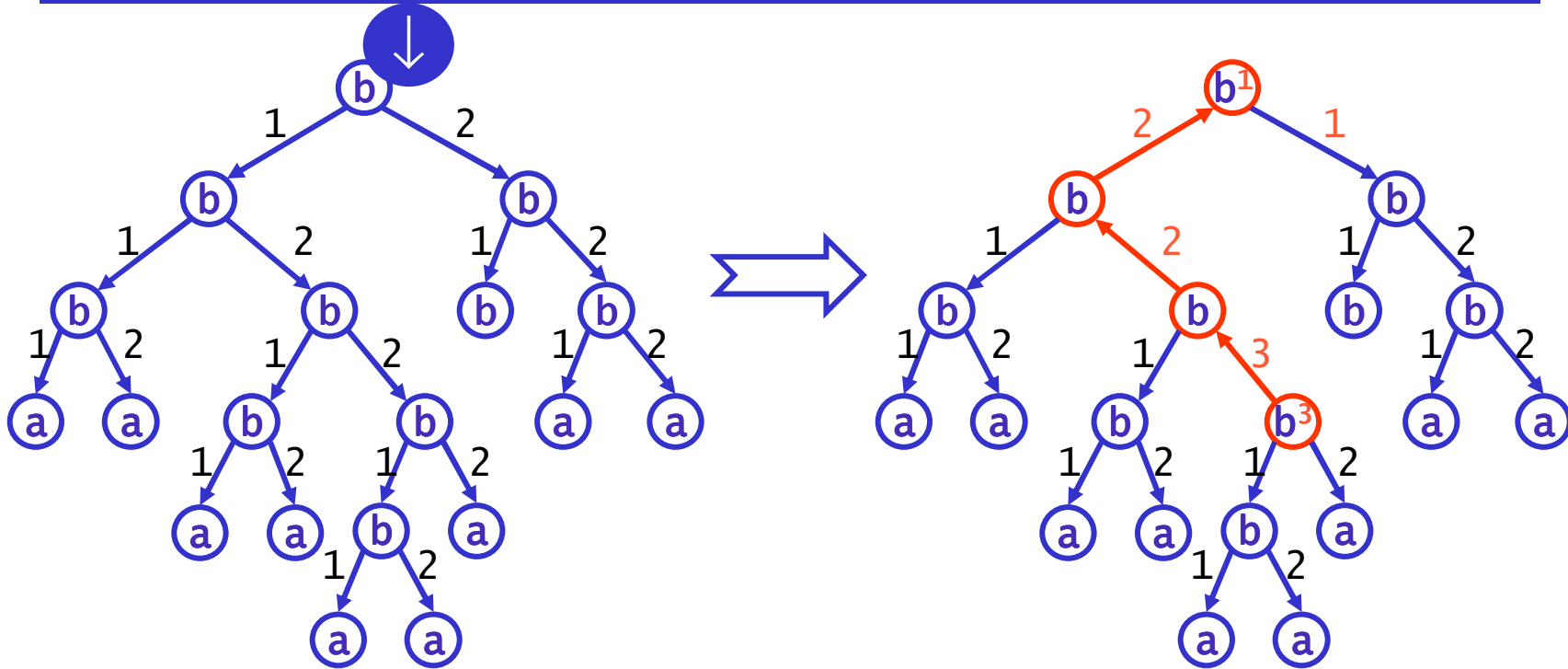


output production

$$(q, \sigma, b, j) \rightarrow \delta(q_1, q_2 \dots q_n)$$



without pebbles
 example: moving the root



walk down

$$(\downarrow, b, -, j) \rightarrow (\downarrow, \text{down}_1)$$

$$(\downarrow, b, -, j) \rightarrow (\downarrow, \text{down}_2)$$

copy up

$$(\uparrow, b, -, 1) \rightarrow b(\uparrow_1, c_2)$$

$$(\uparrow, b, -, 2) \rightarrow b(c_1, \uparrow_2)$$

$$(\uparrow_i, b, -, i) \rightarrow (\uparrow, \text{up})$$

copy down

$$(\text{copy}, a, -, j) \rightarrow a()$$

$$(\text{copy}, b, -, j) \rightarrow b(c_1, c_2)$$

$$(c_i, b, -, j) \rightarrow (\text{copy}, \text{down}_i)$$

$$j=0, 1, 2 \quad i=1, 2$$

Pebble Tree Transducers

$V_k I$ -PTT	visible + invisible	
V_k -PTT	k visible pebbles	Milo et al.
I -PTT	invisible only	
TT	tree-walking (no pebbles)	

Pebble Tree Automata

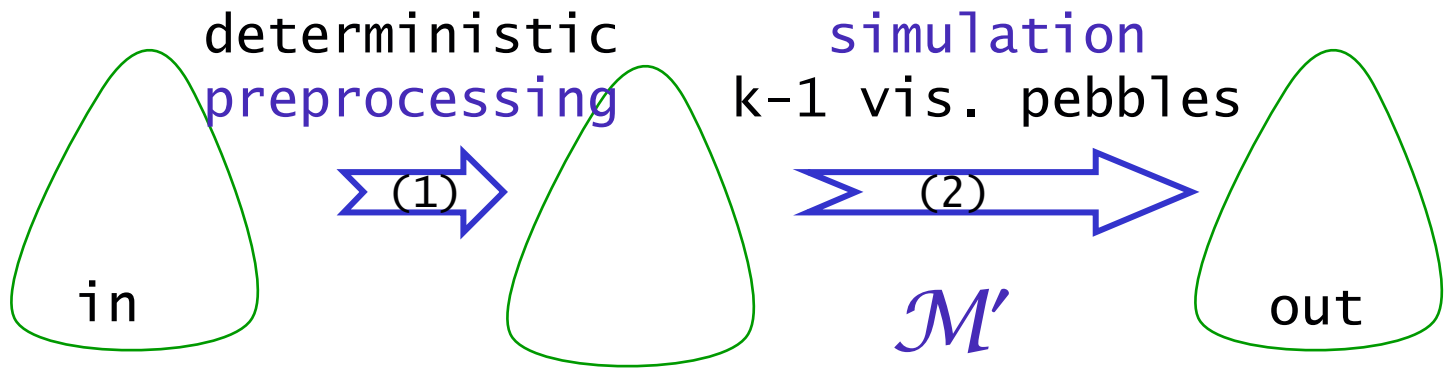
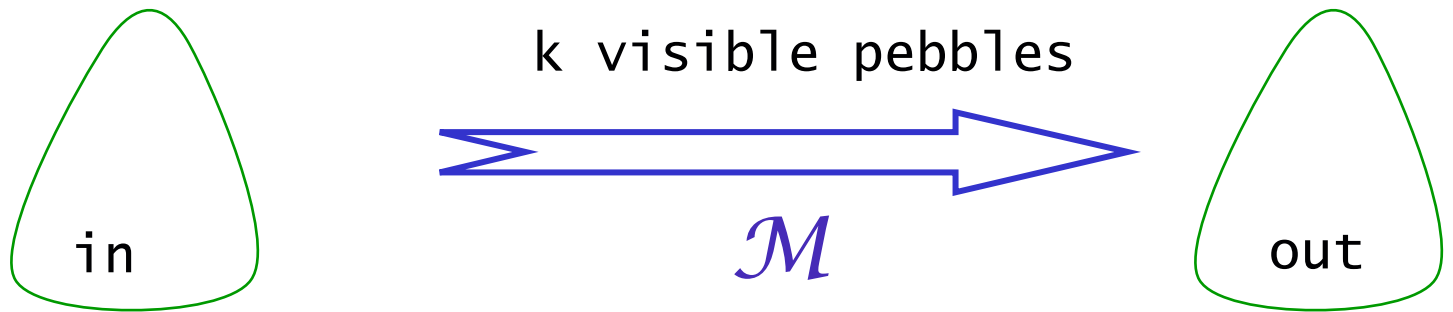
$V_k I$ -PTA
 V_k -PTA
 I -PTA

1. automata with pebbles
2. decomposition
3. typechecking
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7. conclusion



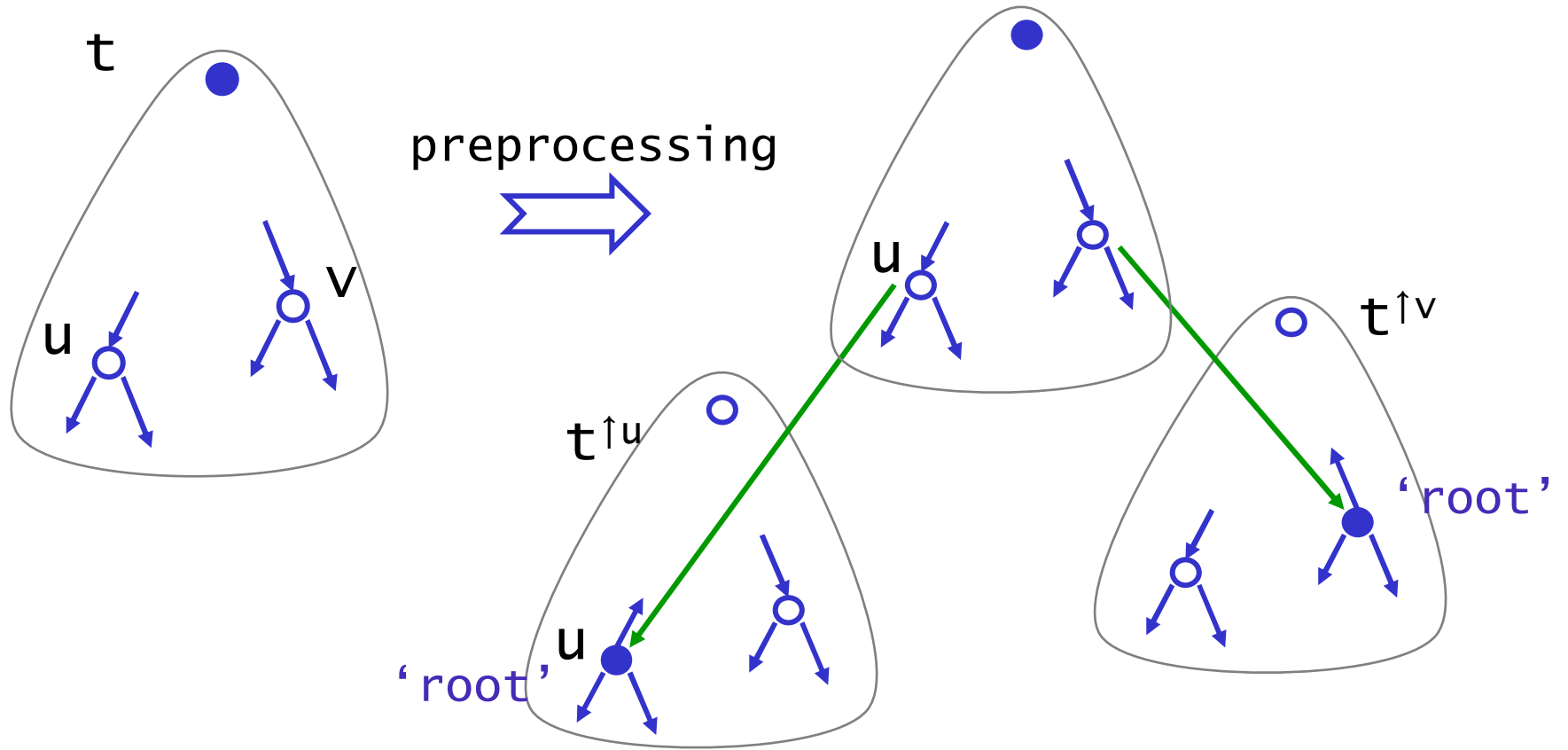
decomposition visible pebbles

$$V_k \text{I-dPTT} \subseteq \text{dTT} \circ V_{k-1} \text{I-dPTT}$$



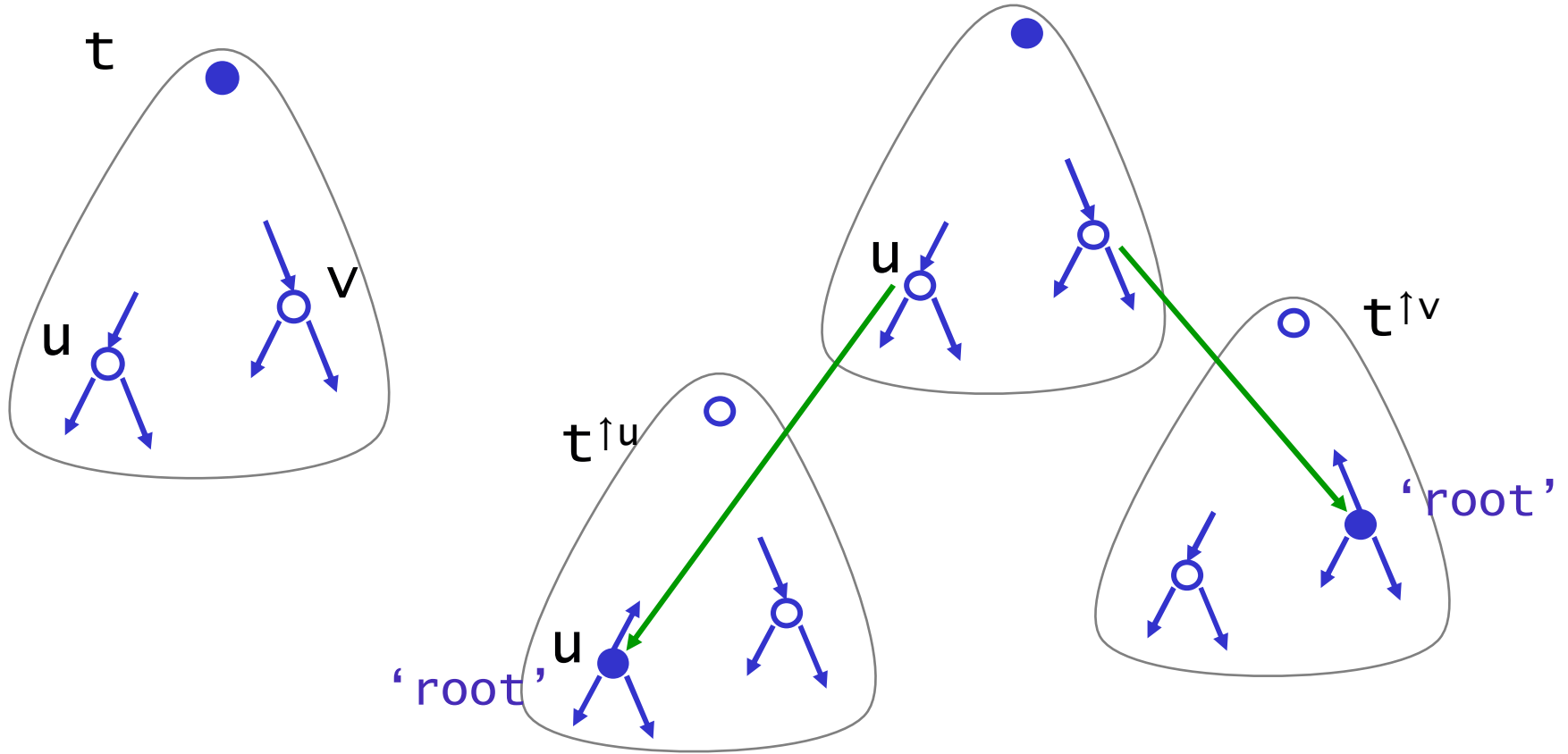
iterate $V_k \text{I-dPTT} \subseteq \text{dTT}^k \circ \text{I-dPTT}$

decomposition (1) *preprocessing*



copying can be done without pebbles

decomposition (2) *simulation*



\mathcal{M}

drop / lift
first visible pebble

\mathcal{M}'

move up /down
into subtree

decomposition

$$V_k \text{I-dPTT} \subseteq \text{dTT} \circ V_{k-1} \text{I-dPTT}$$

$$\text{I-dPTT} \subseteq \text{TT} \circ \text{dTT}$$

(deterministic)

THEOREM

$$V_k \text{-PTT} \subseteq \text{TT}^{k+1}$$

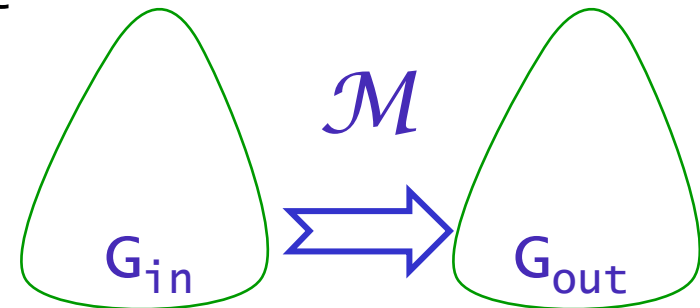
$$V_k \text{I-PTT} \subseteq \text{TT}^{k+2}$$

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inverse type inference

given transducer \mathcal{M} and regular G_{out} ,
 construct regular G_{in} such that
 $L(G_{\text{in}}) = \mathcal{M}^{-1} L(G_{\text{out}})$



Bartha 1982

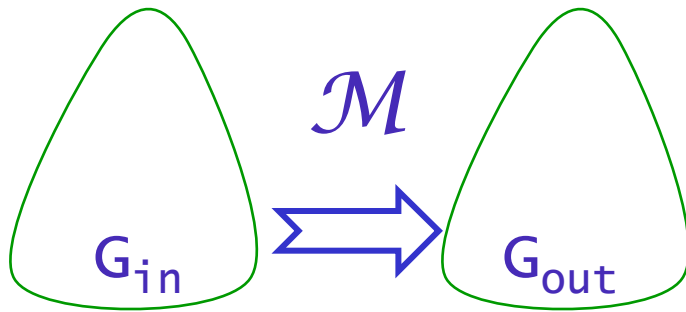
regular tree grammar G for the domain
 of tree transducer \mathcal{M} can be constructed
 in *exponential* time

- inverse type inference is solvable
- \Rightarrow for TT in exponential time
- \Rightarrow for TT^k in k -fold exponential time

type checking complexity

type checking

given transducer \mathcal{M} and regular G_{in}, G_{out} ,
decide whether $\mathcal{M}(L(G_{in})) \subseteq L(G_{out})$



$M(A) \subseteq B$ iff $A \cap M^{-1}(B^c) = \emptyset$
'typechecking' 'inverse type inference'

$$V_k\text{-PTT} \subseteq \text{TT}^{k+1}$$
$$V_k\text{I-PTT} \subseteq \text{TT}^{k+2}$$

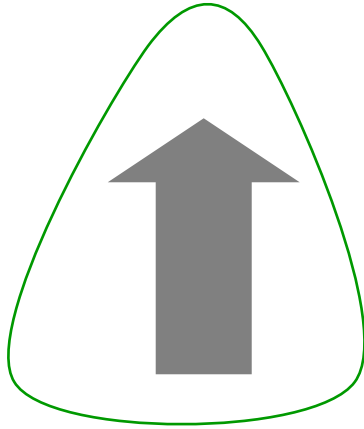
we can typecheck
 $\Rightarrow \text{TT}^k$ in $(k+1)$ -fold exponential time
 $\Rightarrow V_k\text{-PTT}$ in $(k+2)$ -fold exponential time
 $\Rightarrow V_k\text{I-PTT}$ in $(k+3)$ -fold exponential time

invisible pebbles are almost for free!

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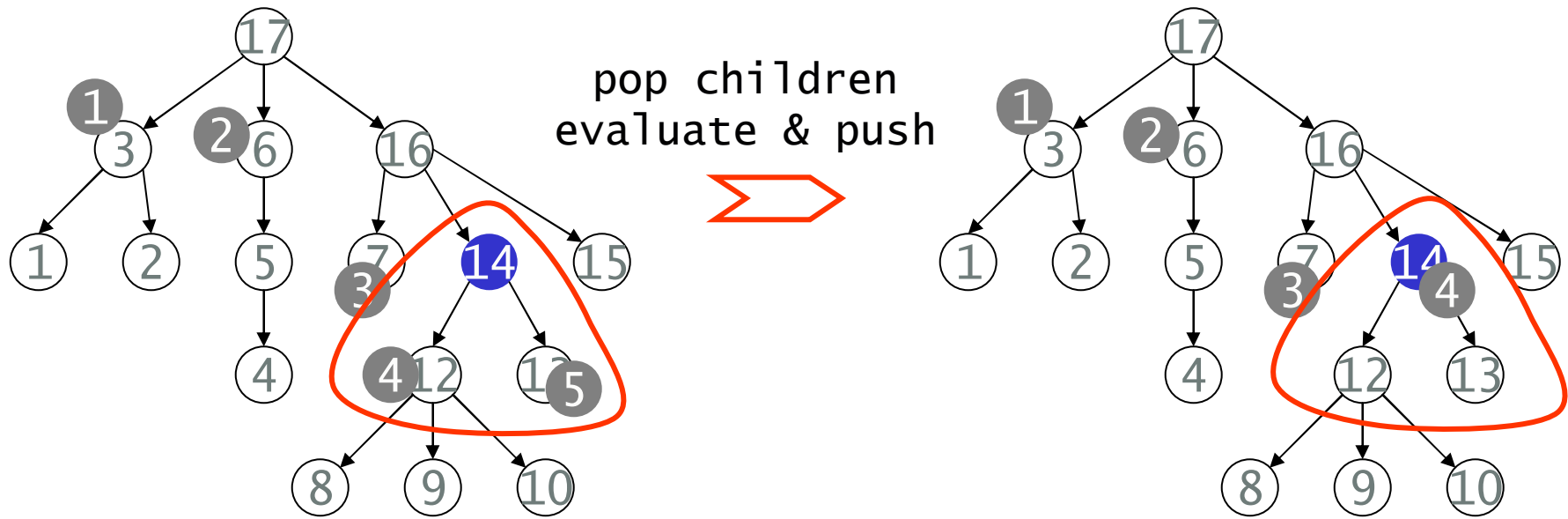


regular trees

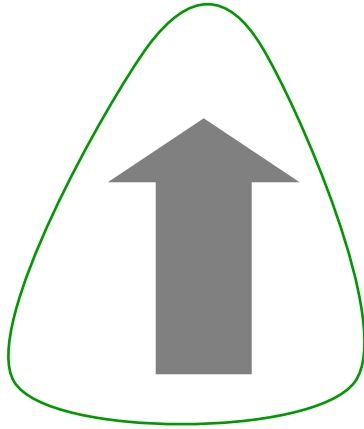


regular tree language
≡ bottom-up tree evaluation
≡ post-order evaluation with stack

$\text{REGT} \subseteq \text{I-PTA}$



regular trees



regular tree language
≡ bottom-up tree evaluation
≡ post-order evaluation with stack

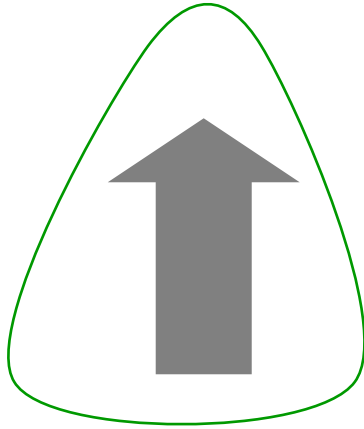
$\text{REGT} \subseteq \text{I-PTA}$

$\text{REGT} \not\subseteq \text{V}_k\text{-PTA}$ Bojańczyk et al.

$\text{V}_k\text{I-PTT} \subseteq \text{TT}^{k+2}$

$\text{V}_k\text{I-PTA} \subseteq \text{REGT}$

regular trees



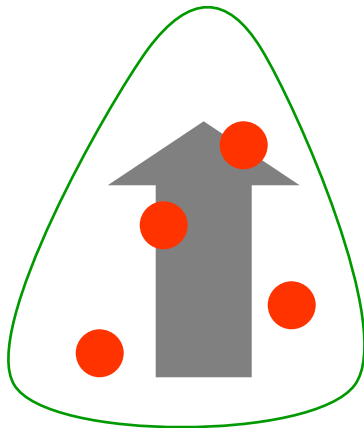
regular tree language
≡ bottom-up tree evaluation
≡ post-order evaluation with stack

$$\text{REGT} \subseteq \text{I-PTA}$$

$$\text{REGT} \not\subseteq \text{V}_k\text{-PTA}$$

$$\text{V}_k\text{I-PTT} \subseteq \text{TT}^{k+2}$$

$$\text{V}_k\text{I-PTA} \subseteq \text{REGT}$$



I-PTA can
- evaluate *marked* trees
- test their visible configuration

1. automata with pebbles
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document navigation

- *Pebble Cat*

caterpillar expressions + pebbles \leftrightarrow I-PTA programs

node expressions
 $\varphi_0 ::= \text{lab}_\sigma \mid \text{isleaf} \mid \text{isroot} \mid$
 $\text{isfirst} \mid \text{islast} \mid \text{pebble}_c$

tests

$\varphi ::= \varphi_0 \mid \neg\varphi \mid \varphi \wedge \varphi$

path expressions

$\alpha_0 ::= \text{child} \mid \text{parent} \mid \text{right} \mid \text{left} \mid$
 $\text{drop}_c \mid \text{lift}$

moves
pebbles

$\alpha ::= \alpha_0 \mid ?\varphi \mid \alpha \cup \alpha \mid \alpha / \alpha \mid \alpha^*$

Kleene

semantics

$[\varphi]_f = \{ (u, \pi), (u, \pi) \mid (u, \pi) \in [\varphi]_f \}$
head pebble stack

document navigation

- *Pebble Cat*

caterpillar expressions + pebbles

↔ I-PTA programs

MSO complete ☺

- *PCat*

↔ V-PTA programs

Goris, Marx LICS'05

- *Pebble XPath*

extends Regular XPath with invisible pebbles

$\varphi ::= \varphi_0 \mid \langle \alpha \rangle \mid \neg \varphi \mid \varphi \wedge \varphi$

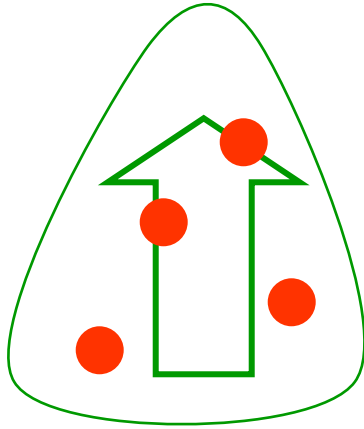
$[\langle \alpha \rangle]_f = \{ (u, \pi) \mid \exists (v, \pi') : ((u, \pi), (v, \pi')) \in [\alpha]_f \}$

⇒ *look-ahead tests*

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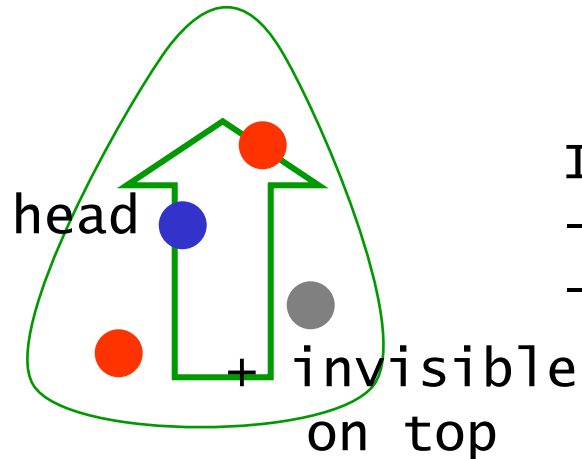
pattern matching



I-PTA can

- evaluate *marked* trees
- test their visible configuration

pattern matching



I-PTA can

- evaluate *marked* trees
- test their ~~visible~~ configuration
observable

VI-PTA can test $\varphi(x_1, \dots, x_n)$ with $n-2$ visible pebbles
(using head)

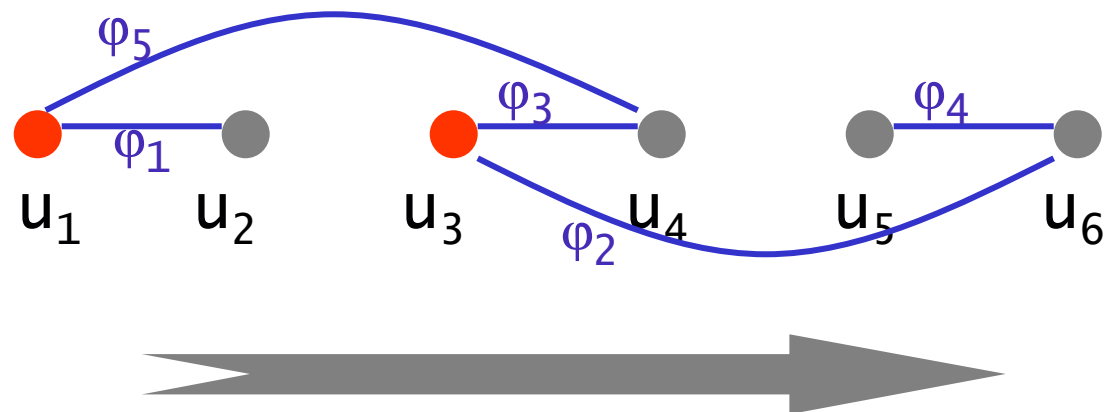
pattern matching

general test $\varphi(x_1, \dots, x_n)$

XQuery **for** x_1, \dots, x_n **with** $\varphi_1 \wedge \dots \wedge \varphi_n$ **return** t
 φ_i binary

example

$$\varphi_1(x_1, x_2) \wedge \varphi_2(x_3, x_6) \wedge \varphi_3(x_4, x_3) \wedge \varphi_4(x_5, x_6) \wedge \varphi_5(x_1, x_4)$$



only 2 visible pebbles!

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- extends known models

V-PTT

Milo, Suciu, Vianu

I-PTT = TL

Maneth et al. PODS'05

DTL document transformation language

- MSO complete
- invisible pebbles are cheap



'tossing Pebbles'

Joost Engelfriet
Hendrik Jan Hoogeboom
Bart Samwel
Leiden NL

thank you ...